

I am interested in solving a large system with block Gauss-Seidel Iterative Method. Suppose I have the following block matrix  $A$  for a system  $Ax = B$ :

$$\begin{pmatrix} A_{EE} & A_{EF} & A_{ET} \\ A_{FE} & A_{FF} & A_{FT} \\ A_{TE} & A_{TF} & A_{TT} \end{pmatrix} \begin{pmatrix} U_E \\ U_F \\ U_T \end{pmatrix} = \begin{pmatrix} f_E \\ f_F \\ f_T \end{pmatrix}$$

where  $V(T) = V_1^E(T) \oplus V_2^F(T) \oplus V_3^T(T)$  and the (small) sub-spaces  $V_1^E(T)$ ,  $V_2^F(T)$ , and  $V_3^T(T)$  are generated by basis functions associated with edges, faces, and cells:

$V_1^E(T)$ on $e_{ij}$	$V_2^F(T)$ on $F_\ell = F_{ijk}$	$V_3^T(T)$
$\lambda_i \nabla \lambda_j - \lambda_j \nabla \lambda_i$	$\lambda_i \lambda_j \nabla \lambda_k - \lambda_j \lambda_k \nabla \lambda_i$ $\lambda_j \lambda_k \nabla \lambda_i - \lambda_k \lambda_i \nabla \lambda_j$	$\lambda_i \lambda_j \lambda_k \nabla \lambda_\ell - \lambda_j \lambda_k \lambda_\ell \nabla \lambda_i$ $\lambda_j \lambda_k \lambda_\ell \nabla \lambda_i - \lambda_k \lambda_\ell \lambda_i \nabla \lambda_j$ $\lambda_k \lambda_\ell \lambda_i \nabla \lambda_j - \lambda_\ell \lambda_i \lambda_j \nabla \lambda_k$

The matrix  $A$  is square. Also the matrices  $A_{EE}$ ,  $A_{FF}$ , and  $A_{TT}$  are square, but not the others.

I am interested in solving the following system:

$$\left( \begin{array}{c|cc} A_{EE} & 0 & 0 \\ \hline A_{FE} & A_{FF} & A_{FT} \\ A_{TE} & A_{TF} & A_{TT} \end{array} \right) \begin{pmatrix} U_E \\ U_F \\ U_T \end{pmatrix} = \begin{pmatrix} f_E \\ f_F \\ f_T \end{pmatrix}$$

So, Is there any way in NGSolve to use the block Gauss-Seidel Iterative Method in solving this system ?. I am grateful for any explanation.